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Growth and spectroscopy of Er³⁺-doped Na₅Y₉F₃₂ (5NaF·9YF₃) crystal

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ABSTRACT

We report on the growth, structure and spectroscopy of an Er^{3+} -doped Na₅Y₉F₃₂ (5NaF·9YF₃) crystal featuring significant inhomogeneous spectral broadening. Single-crystals of Na₅Y₉F₃₂ doped with 0.22 – 9.63 at.% Er^{3+} were grown by the Czochralski method. Er:Na₅Y₉F₃₂ exhibits a cubic fluorite-type structure (a = 5.4881(2) Å for 5.59 at.% Er^{3+} doping). The most intense Raman band of this material is found at ~404 cm⁻¹. Er^{3+} ions in Na₅Y₉F₃₂ exhibit a broad and smooth emission band owing to the ⁴I_{11/2} \rightarrow ⁴I_{13/2} transition with a maximum stimulated-emission cross-section of 0.42×10^{-20} cm² at 2708 nm. According to the Judd-Ofelt analysis, the radiative lifetime of the ⁴I_{11/2} multiplet is 10.0 ms and the luminescence branching ratio $\beta(^{4}I_{11/2} \rightarrow ^{4}I_{13/2})$ is 17.6%. The luminescence lifetimes of the ⁴I_{11/2} and ⁴I_{13/2} Er^{3+} states were studied as a function of the doping concentration. For 5.59 at.% Er doping, they are 7.72 ms and 6.69 ms, respectively, representing a favorable ratio for mid-infrared laser operation.

Keywords: fluoride crystals, sodium-yttrium fluoride, Czochralski method, erbium ions, optical spectroscopy.

1. INTRODUCTION

Crystalline materials formed in binary systems of alkali metal fluorides – rare-earth trifluorides have a good potential as laser host matrices. One example is the NaF – YF₃ binary system. Thoma *et al.* first studied this system and determined the existence of a cubic solid-solution with composition $5\text{NaF}\cdot9\text{YF}_3$ (Na₅Y₉F₃₂) and relatively low melting point at 975 °C [1,2]. Generally, Na₅Y₉F₃₂ is a member of a family of double sodium-yttrium fluoride solid-solution crystals with a general chemical formula of Na_{0.5-x}Y_{0.5+x}F_{2+2x} [3]. Na₅Y₉F₃₂ crystallizes in the cubic class exhibiting a fluorite-type structure (fluorite is the mineral form of CaF₂), even though both components of the binary system (NaF, YF₃) do not exhibit such a structure. The dopant rare-earth ions (RE³⁺) replace for the Y³⁺ ones in the Na₅Y₉F₃₂ lattice. The local symmetry of the surrounding of the Y³⁺ ions (and thus also RE³⁺ ones) is C_{4v} [4]. There are three non-equivalent positions for fluorine anions (F⁻) in Na₅Y₉F₃₂. Previous studies indicate that in Na_{0.5-x}Y_{0.5+x}F_{2+2x} solid-solutions with x = 0 - 0.14, cuboctahedral clusters Y₆F₃₆₋₃₈ are formed [5,6]. This induces a significant inhomogeneous spectral broadening for the dopant RE³⁺ ions leading to smooth and broad absorption and emission spectra (a "glassy-like" spectral behavior) [7]. It is of great interest for broadly tunable and mode-locked lasers.

Erbium ions (Er^{3+}) are attractive for laser emission in the mid-infrared, at 2.8 µm, according to the ${}^{4}I_{11/2} \rightarrow {}^{4}I_{13/2}$ electronic transition. ~2.8 µm lasers are of practical importance for laser surgery. Fluoride crystals are attractive for heavy doping with Er^{3+} ions for mid-infrared laser applications [8-11]. Among them, $Er:CaF_2$ is of particular interest because of the profound rare-earth ion clustering leading to both i) efficient energy-transfer upconversion between the Er^{3+} ions within clusters even at moderate doping levels and ii) broadband emission properties [11,12]. It would be interesting to explore the potential of Er^{3+} -doped fluorite-type Na₅Y₉F₃₂ crystals as laser gain media.

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Fiber Lasers and Glass Photonics: Materials through Applications III, edited by Maurizio Ferrari, Angela B. Seddon, Stefano Taccheo, Proc. of SPIE Vol. 12142, 121420L © 2022 SPIE · 0277-786X · doi: 10.1117/12.2621022 So far, only a few studies were dedicated to rare-earth doped $Na_{0.5-x}Y_{0.5+x}F_{2+2x}$ crystals as laser gain media. Tkachuk *et al.* reported on the mid-infrared laser operation of an Er^{3+} -doped $Na_{0.4}Y_{0.6}F_{2.2}$ (2NaF·3YF₃) crystal [13]. Under pumping by an InGaAs laser diode, an output power of 72 mW at 2.8 µm was achieved with a slope efficiency of only 4%. Excited-state absorption of Er^{3+} ions in $Na_5Y_9F_{32}$ crystals was studied in [14].

In the present work, we report on the growth, structural and spectroscopic study of a disordered Er^{3+} -doped $Na_5Y_9F_{32}$ crystal promising for the development of ~2.8 µm lasers.

2. EXPERIMENTAL

2.1 Crystal growth

Single-crystals of Na₅Y₉F₃₂ (5NaF·9YF₃) doped with 0.2 – 10 at.% Er³⁺ (with respect to Y³⁺, initial composition) were grown by the Czochralski (Cz) method. The growth charge was prepared from a stoichiometric mixture of NaF (purity: 2N), YF₃ and ErF₃ reagents. The rare-earth fluorides (REF₃) were obtained via fluorination of the corresponding oxides (RE₂O₃, 4N) using an excess of NH₄HF₂ solution under heating at 180 °C and the dry cakes were annealed at 650 °C for 4 h under Ar atmosphere to remove the residual NH₄F and moisture. The growth charge was well degassed in a vacuum furnace (10⁻⁵ mbar) by gradual heating up to 300 °C. The crucible was then heated to the temperature slightly higher than the melting point of Na₅Y₉F₃₂ (975 °C) under an Ar + CF₄ atmosphere to ensure that the raw materials are completely molten. For the crystal growth, an oriented seed from undoped Na₅Y₉F₃₂ was used. The pulling rate was 3 mm/h.

The as-grown crystals had a cylindrical shape with uniform cross-section (Φ 12- 15 mm, length: 20 - 25 mm). All the crystals, except the one with the highest doping (10 at.% Er³⁺), were transparent and free of cracks and inclusions. The crystals had a rose coloration due to the Er³⁺ dopant. The actual Er³⁺ doping level was determined by atomic emission spectroscopy (AES): five crystals doped with 0.22, 1.16, 2.0, 5.59 and 9.63 at.% Er³⁺ were studied. E.g., for the 5.59 at.% Er³⁺-doped crystal, the corresponding ion density $N_{\rm Er}$ was 8.23×10^{20} at/cm³.



Figure 1. A photograph of a polished 2.0 at.% Er:Na₅Y₉F₃₂ crystal.



Figure 2. X-ray powder diffraction (XRD) pattern of a 5.59 at.% Er:Na₅Y₉F₃₂ crystal, *blue peaks* – theoretical reflections for undoped Na_{0.39}Y_{0.61}F_{2.22} (PDF card #01-071-5986), *numbers* – Miller's indices (*hkl*).

The phase purity and the crystal structure were confirmed by X-ray powder diffraction (XRD). The XRD pattern was measured with a D8-Advance diffractometer with a lynx-eye detector (opening 2.9463°) using Cu Ka1 ($\lambda = 1.5418$ Å) radiation in the 2θ range of $10 - 90^\circ$ with a step size of 0.02° and a step time of 2 s. The measured XRD pattern for the

5.59 at.% Er:Na₅Y₉F₃₂ crystal is shown in Fig. 2. No other peaks except those belonging to the cubic phase (Na_{0.39}Y_{0.61}F_{2.22}, ICSD card #01-071-5986) were found. The crystal structure of Er:Na₅Y₉F₃₂ was refined by the Rietveld method using the Topas software. Er:Na₅Y₉F₃₂ belongs to the cubic class (sp. gr. O⁵_h - *Fm*-3*m*, No. 225) being isostructural to CaF₂. The calculated lattice constant a = 5.4881(2) Å (the number of formula units in the unit-cell Z = 4), the volume of the unit-cell V = 165.299(3) Å³ and the calculated density $\rho_{calc} = 3.888$ g/cm³.

3. RESULTS AND DISCUSSION

3.1 Raman spectra

The Raman spectra of an undoped and 0.22 at.% Er^{3+} -doped $Na_5Y_9F_{32}$ crystals were measured using a confocal microscope (inVia, Renishaw) equipped with a ×50 objective (Leica) and an Ar⁺ ion laser (457, 488 nm), see Fig. 3. The Raman spectrum of the undoped $Na_5Y_9F_{32}$ crystal exhibits several broad poorly resolved bands with the maxima at 130, 229, 350, 404, 470 and 516 cm⁻¹. The most intense band is found at 404 cm⁻¹. For the 0.22 at.% Er^{3+} -doped crystal, the Raman bands overlap with the Er^{3+} luminescence. Despite this, a similar set of Raman-active modes is observed. The low phonon energy behavior of the $Na_5Y_9F_{32}$ host matrix is advantageous for Er^{3+} doping with the goal of observing mid-IR emission.



Figure 3. Unpolarized Raman spectra of undoped (*blue*) and 0.22 at.% Er doped (*red*) $Na_5Y_9F_{32}$ crystals, *numbers* denote the Raman frequencies in cm⁻¹.

3.2 Optical absorption

The absorption spectrum of the 5.59 at.% Er:Na₅Y₉F₃₂ crystal was measured using a spectrophotometer (Lambda 1050, Perkin Elmer), Fig. 4(a). The absorption bands are related to transitions of Er^{3+} ions from the ground-state, ${}^{4}\text{I}_{15/2}$, to excited-states ranging from ${}^{4}\text{I}_{13/2}$ up to ${}^{2}\text{G}_{7/2}$. Here, the assignment is after Carnall *et al.* [15].



Figure 4. (a) An overview absorption spectrum of a 5.59 at.% Er:Na₅Y₉F₃₂ crystal; (b) absorption cross-section spectra for the ${}^{4}I_{15/2} \rightarrow {}^{4}I_{11/2}$ transition of Er³⁺ ions in the Na₅Y₉F₃₂ and CaF₂ cubic crystals.

For the ${}^{4}I_{15/2} \rightarrow {}^{4}I_{11/2}$ transition which is typically used for pumping of Er³⁺-doped materials, e.g., by using commercial InGaAs laser diodes, the peak absorption cross-section ($\sigma_{abs} = \alpha_{abs}/N_{Er}$) is 0.16×10^{-20} cm² at 969.3 nm corresponding to a

large absorption bandwidth (full width at half maximum) of ~18 nm, see Fig. 4(b). As compared to another cubic crystal exhibiting a "glassy-like" spectroscopic behavior, Er:CaF₂, Fig. 4(b), Er:Na₅Y₉F₃₂ provides lower absorption cross-sections while less structured absorption band. The broadband absorption properties of Er:Na₅Y₉F₃₂ are of practical importance for diode-pumping.

The transition intensities of Er^{3+} ions in Na₅Y₉F₃₂ were determined based in the framework of the standard Judd-Ofelt (J-O) theory based on the measured absorption spectrum [16,17]. The obtained intensity parameters are $\Omega_2 = 2.314$, $\Omega_4 = 0.673$ and $\Omega_6 = 1.002$ [10⁻²⁰ cm²]. Using these parameters, the probabilities of spontaneous radiative transitions $A^{\Sigma}_{calc}(JJ')$, the luminescence branching ratios $\beta(JJ')$ and the radiative lifetimes of the excited-states τ_{rad} were then calculated, Table 1. For the upper laser manifold (⁴I_{11/2}), the radiative lifetime is as long as 9.99 ms and the luminescence branching ratio corresponding to emission in the mid-IR, $\beta(^{4}I_{11/2} \rightarrow ^{4}I_{13/2})$ is relatively high, 17.6%.

Table 1. Probabilities of spontaneous radiative transitions of Er^{3+} ions in Na₅Y₉F₃₂ calculated using the standard J-O theory ($\langle \lambda_{em} \rangle$ - mean emission wavelength, $\beta(JJ')$ – luminescence branching ratios, $A^{\Sigma}_{calc}(JJ')$ –probabilities of radiative transitions, ED: electric dipole, MD: magnetic dipole, A_{tot} – total probabilities, τ_{rad} – radiative lifetimes).

$\begin{array}{c} \text{Transition} \\ J \rightarrow J' \end{array}$		<λ _{em} >, nm	β(JJ')	$A^{\Sigma}_{\text{calc}}(\mathbf{J}\mathbf{J}'),$ s ⁻¹	$A_{\text{tot}},$ s ⁻¹	$ au_{ m rad},$ ms
${}^{4}I_{13/2} \rightarrow$	⁴ I _{15/2}	1532.3	1.000	63.22 ^{ED} +31.98 ^{MD}	95.20	10.50
${}^{4}I_{11/2} \rightarrow$	${}^{4}I_{13/2} \\ {}^{4}I_{15/2}$	2745.7 983.5	0.176 0.824	$\frac{10.48^{\text{ED}} + 7.12^{\text{MD}}}{82.45^{\text{ED}}}$	100.05	9.99

3.3 Mid-infrared luminescence

The spectra of mid-IR luminescence were measured using an optical spectrum analyzer (Yokogawa AQ6376E) purged with N₂ gas to diminish the effect of the structured water vapor absorption in air and a zirconium fluoride (ZrF₄) fiber. As an excitation source, we used a Ti:Sapphire laser tuned to 970 nm. The stimulated-emission (SE) cross-sections, σ_{SE} , for the ${}^{4}I_{11/2} \rightarrow {}^{4}I_{13/2}$ transition of Er³⁺ ions in the Na₅Y₉F₃₂ crystal were calculated using the Füchtbauer–Ladenburg (F-L) formula [18]:

$$\sigma_{\rm SE}(\lambda) = \frac{\lambda^5}{8\pi < n^{>2} \tau_{\rm rad} c} \frac{\beta(JJ')W'(\lambda)}{\int \lambda W'(\lambda) d\lambda},$$

where, λ is the light wavelength, $\langle n \rangle$ is the refractive index at the mean emission wavelength $\langle \lambda_{em} \rangle$, τ_{rad} is the radiative lifetime of the emitting state (⁴I_{11/2}) and β (JJ') is the branching ratio, *c* is the speed of light and *W*'(λ) is the luminescence spectrum corrected for the spectral response of the set-up. For the Er:Na₅Y₉F₃₂ crystal, $\langle n \rangle = 1.470$, $\tau_{rad} = 9.99$ ms and β (JJ') = 17.6%, according to the Judd-Ofelt analysis, cf. Table 1.



Figure 5. Stimulated-emission (SE) cross-sections, σ_{SE} , for the ${}^{4}I_{11/2} \rightarrow {}^{4}I_{13/2}$ transition of Er^{3+} ions in the Na₅Y₉F₃₂ and CaF₂ cubic crystals.

The calculated σ_{SE} spectrum for the Er:Na₅Y₉F₃₂ crystal is shown in Fig. 5. This material exhibits a broad and smooth emission band (a "glassy"-like behavior) spanning from 2.55 to 3.05 µm with a maximum $\sigma_{SE} = 0.42 \times 10^{-20}$ cm² at 2708

nm and another intense peak at a longer wavelength, 2795 nm ($\sigma_{SE} = 0.33 \times 10^{-20} \text{ cm}^2$). For comparison, in the same figure, we show the σ_{SE} spectrum for the Er:CaF₂ crystal. The spectra of both crystals are similar in shape. Due to the longer radiative lifetime of the ${}^{4}I_{11/2}$ Er³⁺ state in Na₅Y₉F₃₂, the absolute values of SE cross-sections for this material are lower than those for Er:CaF₂.

3.4 Luminescence dynamics

The luminescence dynamics was studied employing a ns optical parametric oscillator (Horizon, Continuum), a 1/4 m monochomator (Oriel 77200), a fast InGaAs detector and an 8 GHz digital oscilloscope (DSA70804B, Tektronix). The decay curves of luminescence from the ${}^{4}I_{11/2}$ and ${}^{4}I_{13/2}$ states of Er^{3+} ions in the 5.59 at.% Er:Na₅Y₉F₃₂ crystal measured under resonant excitation are shown in Fig. 6 plotted in a semi-log scale. The luminescence decay was studied using finely powdered crystal samples to reduce the effect of radiation trapping (reabsorption). The luminescence decay times τ_{lum} amount to 7.72 ms (${}^{4}I_{11/2}$) and 6.69 ms (${}^{4}I_{13/2}$), representing a favorable ratio for mid-IR laser operation.

Table 2 summarizes the τ_{lum} values as a function of the Er³⁺ doping concentration. At a very low doping level (0.22 at.% Er³⁺), the lifetime of the lowest excited-state, ⁴I_{13/2}, is close to the radiative value determined using the J-O theory. For the next excited state, ⁴I_{11/2}, the τ_{lum} values is relatively close to the radiative lifetime indicating a weak non-radiative relaxation in agreement with the low phonon energy behavior of the host matrix. Upon Er³⁺ doping, the ⁴I_{13/2} lifetime decreases fast while the ⁴I_{11/2} one remains nearly constant. This highlights the potential of highly Er³⁺-doped Na₅Y₉F₃₂ crystals for laser operation in the mid-IR. Considering the deteriorated optical quality of 10 at.% Er³⁺-doped crystals, the doping levels about 4 – 7 at.% appear to be promising for laser experiments.



Figure 6. Luminescence decay curves for Er^{3+} ions in an 5.59 at.% Er:Na₅Y₉F₃₂ crystal: (a) decay from the ⁴I_{11/2} state, $\lambda_{\text{exc}} = 970 \text{ nm}$, $\lambda_{\text{lum}} = 1015 \text{ nm}$; (b) decay from the ⁴I_{13/2} state, $\lambda_{\text{exc}} = 1480 \text{ nm}$, $\lambda_{\text{lum}} = 1535 \text{ nm}$.

Er content (at.%)	0.22	1.16	2	5.59	9.63
$\tau_{\rm lum}({}^{4}{\rm I}_{11/2})$, ms	6.78	6.55	6.65	7.72	6.41
$\tau_{\rm lum}({}^{4}{ m I}_{13/2}),{ m ms}$	10.51	10.20	8.53	6.69	3.79

Table 2. Luminescence decay lifetimes τ_{lum} of the ${}^{4}I_{11/2}$ and ${}^{4}I_{13/2}$ Er³⁺ manifolds in Na₅Y₉F₃₂ as a function of doping level.

4. CONCLUSIONS

To conclude, Er^{3+} -doped $Na_5Y_9F_{32}$ (5NaF·9YF₃) fluoride crystal is an attractive material for mid-infrared lasers emitting around 2.8 µm according to the ${}^{4}I_{11/2} \rightarrow {}^{4}I_{13/2}$ transition. This crystal possesses a cubic (fluorite-type) structure. The Er^{3+} ions in $Na_5Y_9F_{32}$ exhibit significant inhomogeneous spectral broadening leading to broad and smooth ("glassy-like") absorption and emission spectral bands. The low-phonon-energy behavior of the host matrix (the most intense Raman band for undoped $Na_5Y_9F_{32}$ is found at ~404 cm⁻¹) determines relatively long luminescence lifetimes of the upper laser manifold (${}^{4}I_{11/2}$), about 6-7 ms. A favorable ratio of the upper-to-lower laser level lifetimes is reached already at moderate Er^{3+} doping levels (~5 at.%).

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